

Alg. 2 Warm Up #12-4

Unit Circle Quiz first.

Find all the angles between 0 and 2π that are solutions to the following equation. Answer in exact radians.

1. $\sin x = \frac{\sqrt{3}}{2}$

2. $\cos \theta = -\frac{\sqrt{2}}{2}$

3. $\tan x = -1$

4. $\tan \theta = \frac{\sqrt{3}}{3}$

5. $\sin \theta = -1$

6. $\cos x = 0$

Get organized and staple up:

Week 12 Classwork

Warm up on top

7- # 139 ---> 142

Classwork turned in tomorrow after a short warm up.

HW Questions:

Convert from radians \leftrightarrow degrees (No calculator)

1. $\frac{3\pi}{2}$

2. $\frac{4\pi}{9}$

3. 100°

4. 36°

Find the period, amplitude, equation for the line of oscillation (the midline), consider any reflections or shifts and sketch the graph:

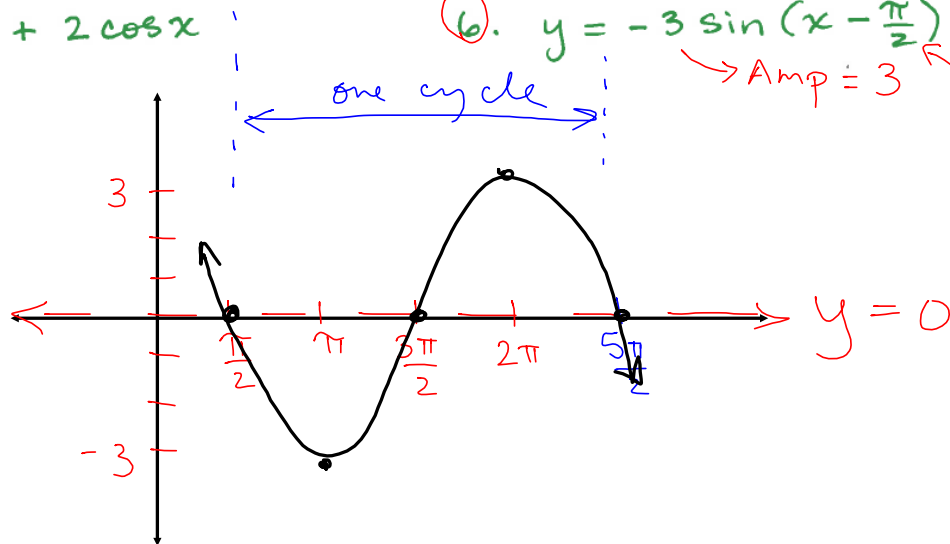
5. $y = 4 + 2 \cos x$

6. $y = -3 \sin(x - \frac{\pi}{2})$

\swarrow $\text{Per} = 2\pi$

\swarrow $\text{Amp} = 3$

\swarrow $2 + \frac{\pi}{2}$



7. $y = \sin 2x + 1$

Per = π

Amp = 1

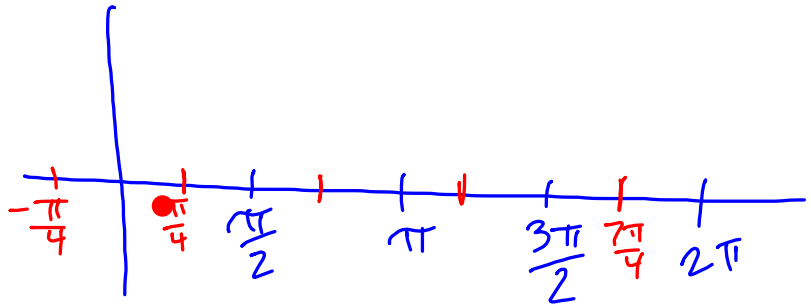
line of Osc $y = 1$

$b = 2$

$\frac{2\pi}{2}$

8. $y = 3 + \sin(x + \frac{\pi}{4})$

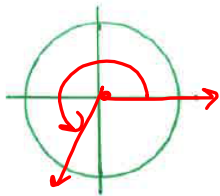
up 3 \rightarrow line of osc $\rightarrow y = 3$
left $\frac{\pi}{4}$ Amp = 1 Per = 2π



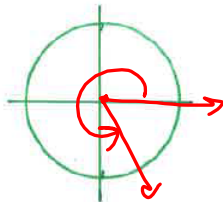
graph the first
cycle between $-\frac{\pi}{4}$
and $\frac{7\pi}{4}$

Draw the following angles on the unit circle:

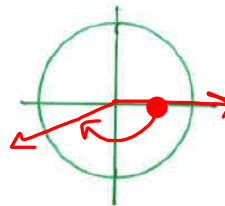
9. $\frac{4\pi}{3}$



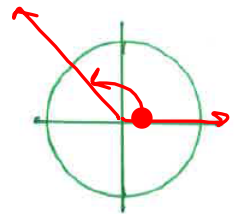
10. $\frac{10\pi}{6} = \frac{5\pi}{3}$



11. $-\frac{5\pi}{6}$



12. $\frac{3\pi}{4}$



Use your unit circle to find:

13. $\sin \frac{7\pi}{4}$

14. $\cos \frac{4\pi}{3}$

15. $\tan \frac{\pi}{2}$

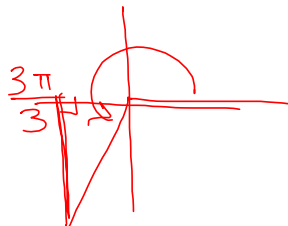
16. $\sin(-\frac{\pi}{6})$

$\frac{1}{0}$
undefined

Same as

$\frac{11\pi}{6}$

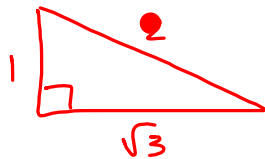
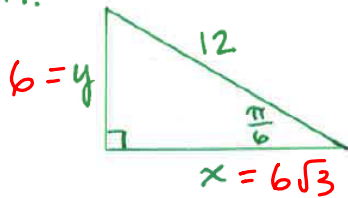
$-\frac{1}{2}$



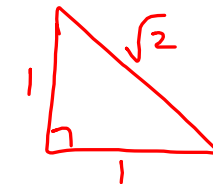
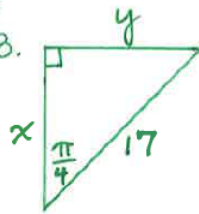
$(-\frac{1}{2}, -\frac{\sqrt{3}}{2})$ $\frac{4\pi}{3}$

Find x & y exact:

17.



18.



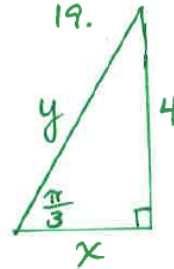
$$\text{hyp} = \text{leg}(\sqrt{2})$$

$$17 = x\sqrt{2}$$

$$x = \frac{17}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}}$$

$$x = \frac{17\sqrt{2}}{2}$$

19.



20.

$$\text{If } \cos \theta = -\frac{\sqrt{3}}{2}$$

Find θ

$$\text{long leg} = \text{sh. leg}(\sqrt{3})$$

$$4 = x(\sqrt{3})$$

$$\frac{4}{\sqrt{3}} = x$$

$$x = \frac{4\sqrt{3}}{3}$$

double for hypotenuse!

Describe the transformations of the parent graph to get:

21. $y = -2 + 4 \cos(2x - \pi)$

Annotations:
 - -2 : down 2
 - 4 : vertical stretch
 - 2 in $\cos(2x - \pi)$: horizontal compression by $\frac{1}{2}$
 - $-\pi$: horizontal shift right by $\frac{\pi}{2}$

reflection in the x-axis

22. $y = -\frac{1}{3} \sin x + 8$

Annotations:
 - $-\frac{1}{3}$: reflection in the x-axis and vertical compression by $\frac{1}{3}$
 - 8 : up 8

23. $y = \tan(x - \frac{\pi}{6}) - 4$

24. $y = \frac{2}{3} \cos(4x + \pi)$

Annotations:
 - $\frac{2}{3}$: vertical compression by $\frac{2}{3}$
 - 4 in $\cos(4x + \pi)$: horizontal compression by $\frac{1}{4}$
 - $+\pi$: horizontal shift left by $\frac{\pi}{4}$

Solve. Answer exact & simplified.

25. $3^{x+5} \cdot 9 = 3^{4x}$

$$3^{x+5} \cdot 3^2 = 3^{4x}$$

$$3^{x+7} = 3^{4x}$$

$$x+7 = 4x$$

$$7 = 3x$$

$$\boxed{x = \frac{7}{3}}$$

26. $4 \log_3 2 = \log_3 x + \log_3 2x$

$$\log_3 2^4 = \log_3 2x^2$$

$$16 = 2x^2$$

$$x^2 = 8$$

$$x = \pm\sqrt{8}$$

$$x = \pm 2\sqrt{2}$$

extraneous

$$\boxed{x = 2\sqrt{2}}$$



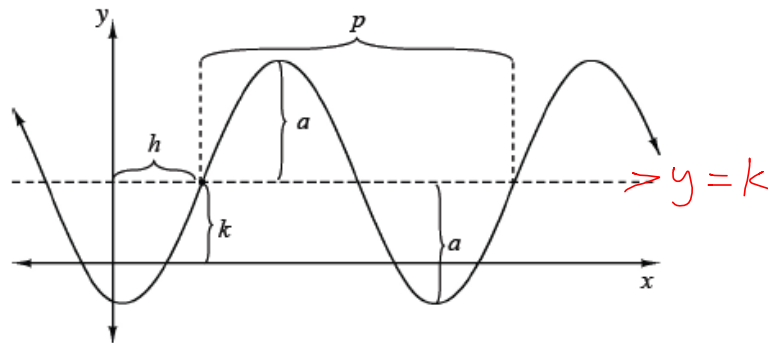
MATH NOTES

METHODS AND MEANINGS

p. 360

General Equation for Sine Functions

The general equation for the **sine function** is $y = a \sin[b(x - h)] + k$.



Per
 $= \frac{2\pi}{b}$ \leftarrow The **amplitude** (half of the distance between the highest and the lowest points) is a . *Vertical stretch or compression*
 The **period** is the length of one cycle. It is labeled p on the graph.

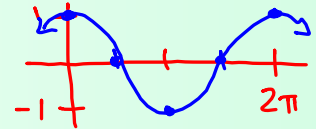
The number of cycles in 2π is b .

The **horizontal shift** is h .

The **vertical shift** is k . The **midline** is $y = k$.

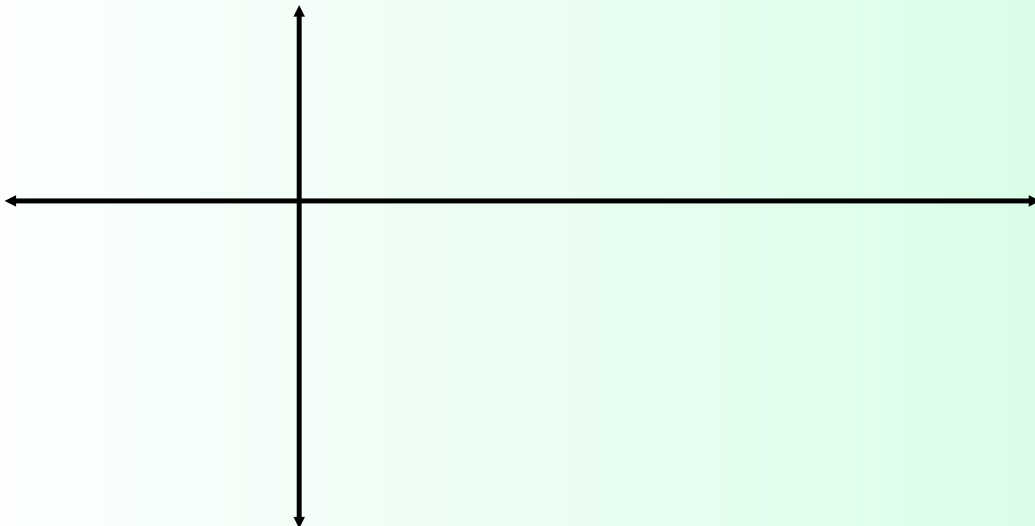
Practice:

Parent: $y = \cos x$



Describe the transformations of $y = \cos x$ that give us $y = 3 \cos (2x - \pi) - 2$, then graph one cycle.

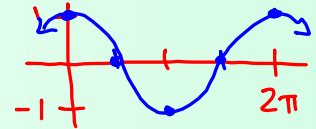
Label the line of oscillation.



Practice:

Parent • $y = \cos x$

vertical stretch of 3



Describe the transformations of $y = \cos x$ that give us $y = 3 \cos (2x - \pi) - 2$, then graph one cycle.

$2(x - \frac{\pi}{2})$ → down 2
 $2 + \frac{\pi}{2}$

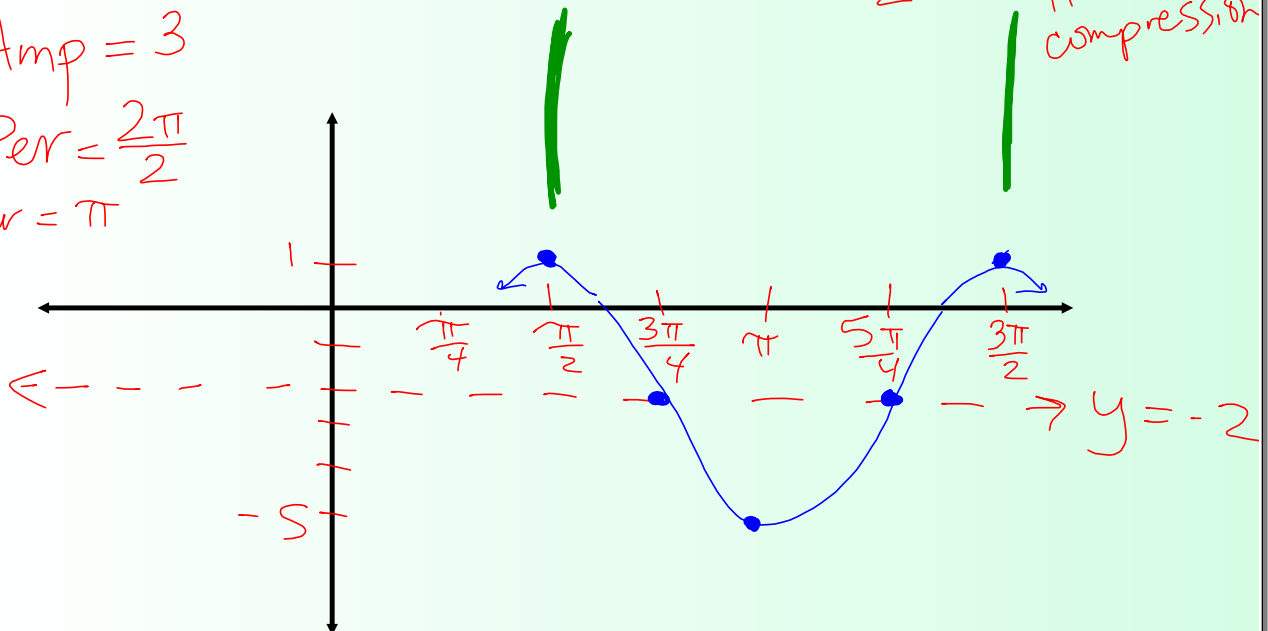
Label the line of oscillation.

Horiz compression

Amp = 3

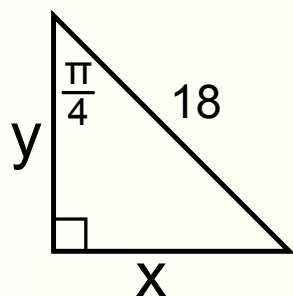
Per = $\frac{2\pi}{2}$

per = π

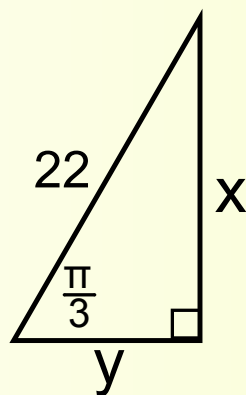


Find x and y , exact and simplified.

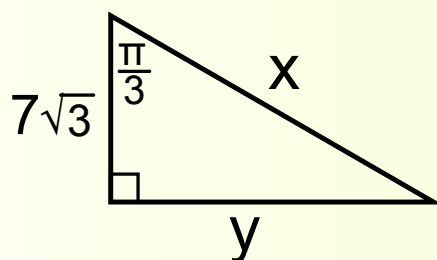
1)



2)

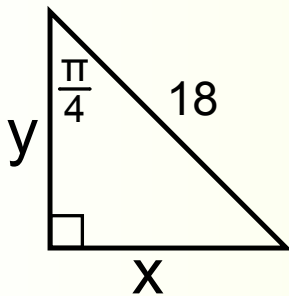


3)



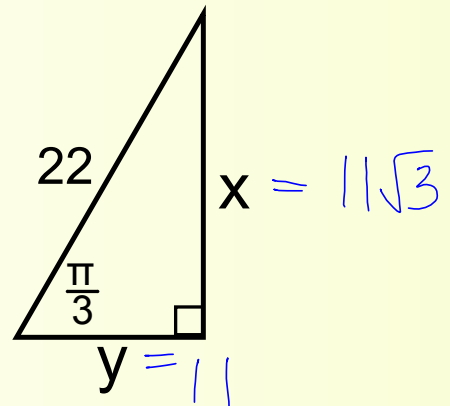
Find x and y, exact and simplified.

1)

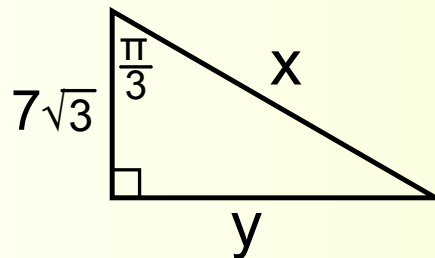


$$\begin{aligned} \text{hyp} &= \text{leg}(\sqrt{2}) \\ 18 &= x\sqrt{2} \\ \text{solve for } x \\ x &= y = 9\sqrt{2} \end{aligned}$$

2)



3)



$$\begin{aligned} \text{long leg} &= (\text{sh. leg})\sqrt{3} \\ y &= 7\sqrt{3} \cdot \sqrt{3} \\ y &= 21 \end{aligned}$$

$$\begin{aligned} \text{hyp} &= 2(\text{sh. leg}) \\ x &= 2(7\sqrt{3}) \\ x &= 14\sqrt{3} \end{aligned}$$

Practice:

1) $\log_2(5x + 6) = 3$

2) $\log_4(x - 6) + \log_4 x = 2$

3) $2 \log_3(x + 1) = 2$

Practice:

1) $\log_2(5x + 6) = 3$

$$2^3 = 5x + 6$$

$$8 = 5x + 6$$

$$2 = 5x$$

$$x = \frac{2}{5}$$

3) $(2) \log_3(x + 1) = 2$

$$\log_3(x + 1)^2 = 2$$

$$3^2 = x^2 + 2x + 1$$

$$0 = x^2 + 2x - 8$$

$$0 = (x + 4)(x - 2)$$

$$x = -4, 2$$

2) $\log_4(x - 6) + \log_4 x = 2$

$$\log_4(x^2 - 6x) = 2$$

$$4^2 = x^2 - 6x$$

$$0 = x^2 - 6x - 16$$

$$0 = (x - 8)(x + 2)$$

$$x = 8, -2$$

HW: Checkpoint 10,
problems are on p. CP 25

1 - 25 odd

In the checkpoint section, back of the book.
This is final exam review of logs.

Chapter Test: Tomorrow
(No calculator)